

# Lecture 28

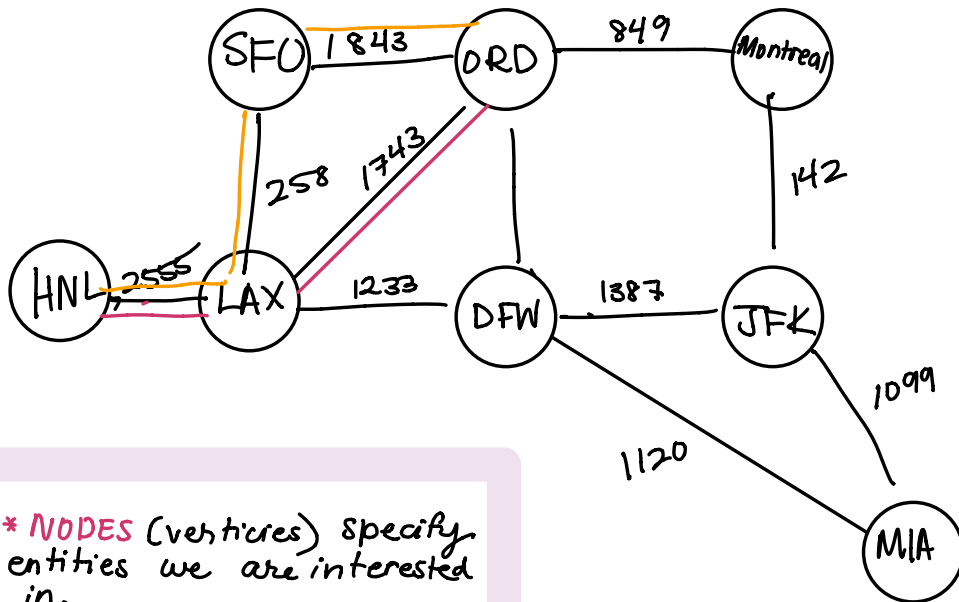
MOTIVATION- visualize flight routes in North America

- natural representation is a graph

① Create Series of nodes (or vertices)  
w/ each node representing a city

- each node is airport code

② Connect any 2 cities (nodes) which  
have a flight route b/w them w/  
a line (called an edge)



\* **NODES** (vertices) specify entities we are interested in.

\* **EDGES** - Specify relationships b/w entities

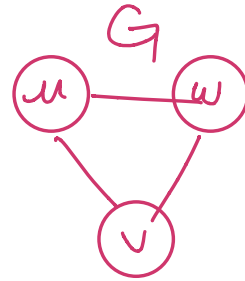
Def. A graph  $G = (V, E)$  is a finite set of vertices  $V$ , and a finite set of edges  $E$ , where each edge  $(u, v)$  connects 2 vertices,  $u$  and  $v$

① Ex. we have

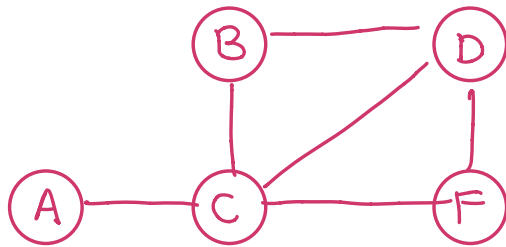
$$G = (V, E)$$

Vertices  $V = \{u, v, w\}$

Edges  $E = \{(u, v), (v, w), (w, u)\}$



②

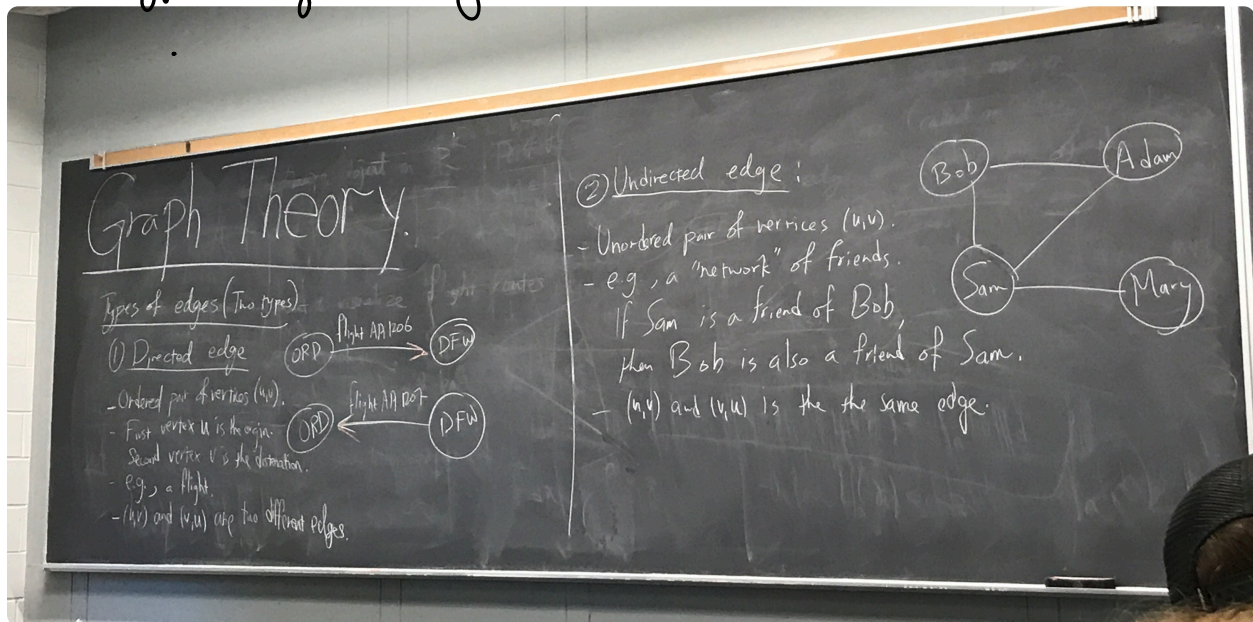


$$G = (V, E)$$

Vertices  $V = \{a, b, c, d, e, f\}$

Edges  $E = \{(a, c), (b, c), (b, d), (c, d), (d, e), (e, f), (c, f)\}$

# Types of Edges



## Types of Graphs

### ① Directed Graph

- all edges are directed
- route network

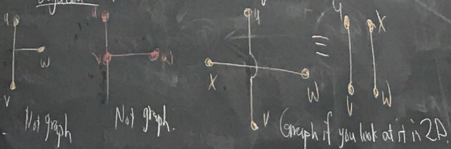
### ② Undirected Graph

- all edges are undirected
- friend network

# Graph Theory

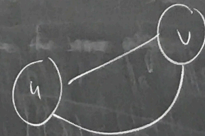
## Terminology

Def. Two vertices,  $u$  and  $v$ , of a graph are adjacent if there exists an edge  $(u, v)$ .



Def. A self-loop is an edge  $(u, u)$ .

Def. Multi-edges (or parallel edges) are edges that have the same endpoints (in undirected graph) or the same origin and destination (in directed graph).



Def. If a graph does not have parallel edges and self-loops, then it is called simple.

Def. A multi-graph can have multiple edges between the same two vertices and self loops.

In this course, we deal almost exclusively with simple graphs.

