



Student's Name: .....

Instructor's Name: .....

Student's Number: .....

Class Time: .....

Second Exam  $\diamond$  Calculus I (0301101)  $\diamond$  Fall 2016

Note: This exam is composed of 15 questions. You have 60 minutes to finish

For questions 1-12, fill in the blank with the correct answer. Only correct answer count. [1.5 point each].

1. If  $4x^2 + 2xy + y^2 = 12$ , then  $\frac{dy}{dx}$  at the point  $(1, 2)$  is equal to .....

2.  $\lim_{h \rightarrow 0} \frac{8(1+h)^8 - 8}{h} = \dots\dots\dots$

3. The equation of the tangent line to the graph of  $y = \sin^{-1}\left(\frac{x}{y}\right)$  at the origin .....

4.  $\frac{d}{dx} [\log_3(x^2 + e^2)] = \dots\dots\dots$

5.  $f(x) = \frac{\sin x}{\sqrt{4-x^2}}$  is continuous on .....

6.  $\lim_{x \rightarrow \frac{\pi}{2}} e^{\sec(x)} = \dots\dots\dots$

7. If  $g(0) = 2$ ,  $g'(0) = 3$  and  $f(x) = \frac{4 - 3e^{2x}}{x + g(x)}$ , then  $f'(0) = \dots\dots\dots$

8.  $\lim_{x \rightarrow 0} \frac{1 - \cos^2(4x)}{x^2} = \dots\dots\dots$

9. If  $f(x) = \sec^3(7^x)$ , then  $f'(x) = \dots\dots\dots$

10. If  $f(x) = \ln(x + 8)$ , then  $\lim_{x \rightarrow 2} \frac{f(x) - f(2)}{x - 2} = \dots\dots\dots$

11. The vertical asymptote of  $f(x) = \frac{x - 2}{x^2 - 5x + 6}$  is  $x = \dots\dots\dots$

12.  $\lim_{x \rightarrow -2} \frac{2x + 4}{|x| + 2} = \dots\dots\dots$

For questions 13-15, sufficient work must be shown to receive credit.

13. [4 points] Find  $\lim_{x \rightarrow -\infty} (\sqrt{x^2 + 3x} + x)$ .

14. [4 points] Use linear approximation to estimate  $\sqrt[3]{1001}$ .

15. [4 points] Differentiate  $f(x) = \frac{\sqrt[4]{x} \sin^9(x)}{(x-1)^7 e^{x^2}}$ .